

1. In class we proved that  $D(\text{EQ}) \geq n$  and  $D(\text{IP}_2) \geq n$ , where  $n$  is the length of the input of Alice and Bob. Show that  $D(\text{EQ}) = n + 1$  (the fooling set argument) and  $D(\text{IP}_2) = n + 1$  (the rank lower bound).
2. Exercise 1.26 of the CC Book: Prove that the size of any 1-monochromatic rectangle of the DISJ function is at most  $2^n$ . Conclude that  $D(\text{DISJ}) = \Omega(n)$ .
3. Exercise 1.31 of the CC Book: Let  $f : X \times Y \rightarrow \{0, 1\}$  be a Boolean function:
  - a). Prove that if  $f$  is such that all the rows of  $M_f$  are distinct, then  $D(f) \geq \log \log |X|$ .
  - b). Prove that  $D(f) \leq \text{rank}(f) + 1$ .